## HEAT TRANSFER IN AGITATED VESSELS



# HEAT TRANSFER IN AGITATED VESSELS 

## GROUP MEMBERS

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2006-Chem-22
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## Problem Statement

A batch polymerization reactor, 1500 mm in diameter and 1800 mm high, has a limpet coil of 18 turns. The inner diameter of the half-pipe is 52.5 mm and the pitch of the coil is 79.5 mm . In Each batch, 2200 kg of the monomer at $25^{\circ} \mathrm{C}$ is charged to the reactor that has to be heated to $80^{\circ} \mathrm{C}$ before the initiator is added to start the polymerization.



## Problem Statement

Heating is done by a hot fluid available at $120^{\circ} \mathrm{C}$. The average viscosity of the hot fluid may be taken as 4 cP , and that of the monomer as 0.7 cP . The vessel is provided with a flat blade turbine agitator (six blade. 0.5 m diameter) which rotates at 150 rpm.

## Problem Statement

The volume of the charge is such that, the liquid surface remains nearly at the level of the top of the limpetted region . The height of the limpeted section $=1464 \mathrm{~mm}$. A fouling factor of $0.0002 \mathrm{~h} \mathrm{~m}^{2}{ }^{\circ} \mathrm{C} / \mathrm{kcal}$ may be taken for both the vessel and the coil side.

Calculate the time required to heat the charge.


## DATA: Reactor \& Coil

| Reactor diameter | 1500 mm |
| :--- | :--- |
| Reactor height | 1800 mm |
| No of turns in coil | 18 |
| Pitch of coil | 79.5 mm |
| Inner diameter of half <br> pipe | 52.5 mm |

## DATA

| Weight of monomer per batch | 2200 kg |
| :--- | :--- |
| Temperature of hot fluid | $120^{\circ} \mathrm{C}$ |
| Final temperature of <br> monomer | $80^{\circ} \mathrm{C}$ |
| Density | $900 \mathrm{~kg} / \mathrm{m}^{3}$ |
| Viscosity of hot fluid | 4 cP |
| Thermal conductivity | $0.28 \mathrm{kcal} / \mathrm{h} \mathrm{m}{ }^{\circ} \mathrm{C}$ |
| Heat capacity | $0.50 \mathrm{kcal} / \mathrm{kg}^{\circ} \mathrm{C}$ |

## DATA: agitator

## FLAT BLADE TURBINE AGITATOR

| No. of blades | 6 |
| :--- | :--- |
| Diameter | 0.5 m |
| Rpm | 150 rpm |

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## SOLUTION

## STRATEGY

## 1- Calculate Internal Heat Transfer Area of the Vessel

2- Calculate the vessel-side heat transfer coefficient

3-Calculate Coil side Heat transfer coefficient

## SOLUTION

## STRATEGY

## 4- Calculate Overall Heat Transfer coefficient

## 5- Calculate Time Required for Batch Heating

## Inside heat transfer area of the vessel

The inside heat transfer area of the vessel

$$
\mathrm{A}_{\mathrm{i}} \quad=\quad \pi \mathrm{D}_{\mathrm{t}} \mathrm{H}
$$

$\mathrm{H}=1464 \mathrm{~mm}$
$\mathrm{D}_{\mathrm{t}}=1500 \mathrm{~mm}$

$$
A=6.9 \mathrm{~m}^{2}
$$

## VESSEL SIDE H.T COEFFICIENT

- Agitator diameter $=0.5 \mathrm{~m}$
- Rpm. = 150

Equation for $\mathrm{h}_{\mathrm{i}}$ is

$$
\mathrm{h}_{\mathrm{i}}=\frac{0.74 \mathrm{x} \mathrm{k} \mathrm{x}(\mathrm{Re})^{0.67}(\operatorname{Pr})^{0.33}}{\mathrm{D}_{\mathrm{t}}}
$$

## VESSEL SIDE H.T COEFFICIENT

- Pr. (Prandtl no.) ${ }^{=}=(0.45)\left(0.7 \times 10^{-3}\right)(3600)$ 0.15
$=7.56$
Re.(Reynold no.) $=\underline{\mathrm{d}^{2} \mathrm{~N} \rho}=\underline{(0.5)^{2}(150 / 60)(850)}$

$$
\begin{aligned}
& \mu \\
= & 7.59 \times 10^{5}
\end{aligned}
$$

## VESSEL SIDE H.T COEFFICIENT

- Putting the values of variables in the equation of $h_{i}$

$$
\begin{aligned}
\mathrm{h}_{\mathrm{i}} \quad & =\frac{0.74 \times 0.15 \times\left(7.59 \times 10^{5}\right)^{0.67}(7.56)^{0.33}}{1.5} \\
& =1256 \mathrm{kcal} / \mathrm{h} \mathrm{~m}^{2} \mathrm{C} \mathrm{C}
\end{aligned}
$$

## COIL SIDE H.T COEFFICIENT

Take the linear velocity of the heat transfer fluid $=1.5 \mathrm{~m} / \mathrm{s}$

Flow area of the coil

$$
=(\pi / 4)(0.0525)^{2}=2.165 \times 10^{-3} \mathrm{~m}^{2}
$$

Flow area of the fluid

$$
\begin{aligned}
& =(1.5)\left(2.165 \times 10^{-3}\right)(3600) \\
& =11.69 \mathrm{~m}^{3} / \mathrm{h}
\end{aligned}
$$

Mass flow rate of the fluid $=\mathrm{W}_{\mathrm{c}}=(11.69)(850)=9936 \mathrm{~kg} / \mathrm{h}$

# COIL SIDE HT COEFFICIENT 

Hydraulic diameter of the limpet coil, $\mathrm{d}_{\mathrm{H}}$

$$
\mathrm{d}_{\mathrm{H}}=\frac{(4)(\pi / 8)\left(\mathrm{d}_{\mathrm{i}}\right)^{2}}{\mathrm{~d}_{\mathrm{i}}+(\pi / 2) \mathrm{d}_{\mathrm{i}}}
$$

$$
=\frac{\pi(0.0525)}{2+\pi}=0.0321 \mathrm{~m}
$$

Coil Reynolds Number

$$
\operatorname{Re}=\frac{\mathrm{Vd}_{\mathrm{H}} \rho}{\mu}=\frac{(1.5)(0.0321)(900)}{4 \times 10^{-3}}=10,820
$$

## COIL SIDE H.T COEFFICIENT

## Prandtl Number of the coil fluid

$$
\operatorname{Pr}=\underline{C}_{\mathrm{p}} \underline{\underline{u}} \mathrm{k}=\frac{(0.5)\left(4 \times 10^{-3}\right)(3600)}{0.28}=25.7
$$

Coil side heat transfer coefficient

$$
\begin{aligned}
& \frac{\mathrm{d}_{\mathrm{e}} \mathrm{~h}_{\mathrm{o}}}{\mathrm{k}}=0.027 \mathrm{x}(\mathrm{Re})^{0.8}(\operatorname{Pr})^{0.33}[1+3.5(\mathrm{de} / \mathrm{dc})] \\
& \mathrm{h}_{0}=1080 \mathrm{kcal} / \mathrm{h} \mathrm{~m} \\
& \\
& 0{ }^{0} \mathrm{C}
\end{aligned}
$$

# Overall Heat Transfer Coefficient 

- $\mathrm{U}=467 \mathrm{kcal} / \mathrm{h} \mathrm{m}{ }^{20} \mathrm{C}$


## TIME REQUIRED

- Given data is
- $\mathrm{W}_{\mathrm{c}}=9936 \mathrm{~kg} / \mathrm{h}$
- $\mathrm{C}_{\mathrm{pc}}=0.5 \mathrm{kcal} / \mathrm{kg}^{\mathrm{O}} \mathrm{C}$
- $\mathrm{W}_{\mathrm{v}}=2200 \mathrm{~kg}$
- $\mathrm{c}_{\mathrm{pv}}=0.45 \mathrm{kcal} / \mathrm{kg}^{\circ} \mathrm{C}$
- inlet temperature of the coil fluid, $\mathrm{T}_{\mathrm{ci}} \quad=120^{\circ} \mathrm{C}$
- initial temperature of the vessel liquid, $\mathrm{T}_{\mathrm{vi}}=25^{\circ} \mathrm{C}$.
- final temperature, $\mathrm{T}_{\mathrm{vf}}=80^{\circ} \mathrm{C}$


## TIME REQUIRED

Putting the values of the various quantities in, we get

$$
\begin{aligned}
& \ln \left(\mathrm{T}-\mathrm{t}_{1} / \mathrm{T}-\mathrm{t}_{2}\right)=\left(\mathrm{W}_{\mathrm{c}} \mathrm{C}_{\mathrm{pc}} / \mathrm{W}_{\mathrm{v}} \mathrm{C}_{\mathrm{pv}}\right)((\mathrm{K}-1) / \mathrm{K}) \\
& \mathrm{K}=\quad \exp \left(\mathrm{U}_{\mathrm{i}} \mathrm{~A}_{\mathrm{i}} / \mathrm{W}_{\mathrm{c}} \mathrm{c}_{\mathrm{p}}\right) \\
& =\quad \exp ((467)(6.9) /(9936)(0.5))=1.913 \\
& \ln (120-25 / 120-80)=(9936)(0.5) /(2200)(0.45)(1.913-1 / 1.913) \mathrm{t} \\
& \mathrm{t}=22 \mathrm{mins}
\end{aligned}
$$

## THANKS

